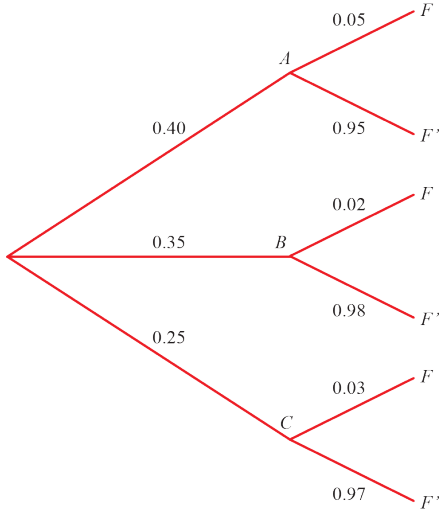
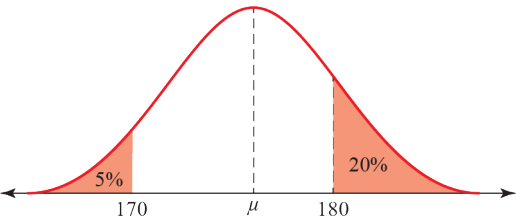


# A level Statistics & Mechanics: Practice Paper I mark scheme

<b>II</b>	<b>Scheme</b>	<b>Marks</b>	<b>AOs</b>	<b>Pearson Progression Step and Progress descriptor</b>
<b>a</b>	$\log n = 0.7606 + 0.0635t$ $c = 10^{0.7606+0.0635t}$ $c = 5.76 \times 1.16^t$ (3 s.f.)	<b>M1</b> <b>M1</b> <b>A1</b>	1.1a 1.1b 1.1b	6th Understand exponential models in bivariate data.
		<b>(3)</b>		
<b>b</b>	$a$ is a constant of proportionality.	<b>A1</b>	3.2a	6th Understand exponential models in bivariate data.
		<b>(1)</b>		
<b>c</b>	Extrapolation/out of the range of the data.	<b>A1</b>	2.4	4th Understand the concepts of interpolation and extrapolation.
		<b>(1)</b>		
				<b>(5 marks)</b>
<b>Notes</b>				

# A level Statistics & Mechanics: Practice Paper I mark scheme

I2	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
<b>a</b>	 <p style="text-align: center;">Let <math>F \sim</math> faulty</p>	<b>B1</b> <b>B1</b> <b>B1</b>	2.5 1.1b 1.1b	3rd Draw and use tree diagrams with three branches and/or three levels.
		<b>(3)</b>		
<b>b</b>	$P(B \cap F') = 0.35 \times 0.98$	<b>M1</b>	1.1b	5th Understand and calculate conditional probabilities in the context of tree diagrams.
	$= 0.343$	<b>A1</b>	1.1b	
		<b>(2)</b>		
<b>c</b>	$P(F) = 0.4 \times 0.05 + 0.35 \times 0.02 + 0.25 \times 0.03$	<b>M1</b>	1.1b	5th Understand and calculate conditional probabilities in the context of tree diagrams.
	$= 0.0345$	<b>A1</b>	1.1b	
		<b>(2)</b>		
<b>d</b>	$P(C F) = \frac{P(C' \cap F)}{P(F)} = \frac{0.4 \times 0.05 + 0.35 \times 0.02}{0.0345} = \frac{0.027}{0.0345}$	<b>M1</b> <b>A1ft</b>	3.1b 1.2	5th Calculate conditional probabilities using formulae.
	$0.7826... \text{ or } \frac{18}{23} \text{ (accept awrt 0.783)}$	<b>A1</b>	1.1b	
		<b>(3)</b>		
<b>(10 marks)</b>				
<b>Notes</b>				

I3	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
a	 <p>bell shaped</p>	B1	1.2	5th Understand the basic features of the normal distribution including parameters, shape and notation.
	170, 180 on axis	B1	1.1b	
	5% and 20%	B1	1.1b	
		(3)		
b	$P(X < 170) = 0.05$ $\frac{170 - \mu}{\sigma} = -1.6449$ $\mu = 170 + 1.6449\sigma$ $P(X > 180) = 0.2$ $\mu = 180 - 0.8416\sigma$ <p>Solving simultaneously gives:</p> $\mu = 176.615\dots \text{ (awrt 176.6) and } \sigma = 4.021\dots \text{ (awrt 4.02)}$	M1	3.3	7th Find unknown means and/or standard deviations for normal distributions.
		B1	3.4	
c	$P(\text{All three are taller than 175 cm}) = 0.656\dots^3$	M1	1.1b	5th Understand informally the link to probability distributions.
	$= 0.282\dots \text{ (using calculator) awrt 0.282}$	A1	1.1b	
		(2)		
<b>(12 marks)</b>				
<b>Notes</b>				

# A level Statistics & Mechanics: Practice Paper I mark scheme

<b>I4</b>	<b>Scheme</b>	<b>Marks</b>	<b>AOs</b>	<b>Pearson Progression Step and Progress descriptor</b>
<b>a</b>	The data seems to follow an exponential distribution.	<b>B1</b>	2.4	6th Understand exponential models in bivariate data.
		<b>(1)</b>		
<b>b</b>	$r = 0.9735$ is close to 1	<b>B1</b>	2.2a	2nd Know and understand the language of correlation and regression.
	which gives a strong positive correlation.	<b>B1</b>	2.4	
		<b>(2)</b>		
<b>c</b>	Model is a good fit with a reason. For example, Very strong positive linear correlation between $t$ and $\log_{10} p$ . The <b>transformed data points</b> lie close (enough) to a straight line.	<b>B2</b>	3.2a	6th Understand exponential models in bivariate data.
		<b>(2)</b>		
				<b>(5 marks)</b>
<b>Notes</b>				
<b>c</b>	B0 for just stating the model is a good fit with no reason.			

# A level Statistics & Mechanics: Practice Paper I mark scheme

I5	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
<b>a</b>	<p style="text-align: center;"><math>T = \text{hand assignments in on time, } D = \text{start assignments on the day they are issued}</math></p>	<b>B1</b> <b>B1</b> <b>B1</b>	2.5 1.1b 1.1b	2nd Draw and use simple tree diagrams with two branches and two levels.
		<b>(3)</b>		
<b>b i</b>	$P(T \cap D) = P(T D) \times P(D)$	<b>M1</b>	3.1b	5th
	$= \frac{3}{5} \times \frac{11}{20}$ $= \frac{33}{100} \text{ or } 0.33$	<b>A1</b>	1.1b	Understand and calculate conditional probabilities in the context of tree diagrams.
		<b>(2)</b>		
<b>b ii</b>	$\frac{3}{5} \times \frac{11}{20} + x \times \frac{2}{5} = \frac{2}{3}$	<b>M1</b>	3.1b	5th Understand and calculate conditional probabilities in the context of tree diagrams.
	$x = \frac{101}{120} \text{ or } 0.841\dots$	<b>A1</b>	1.1b	
	$P(T' \cap D') = \frac{2}{5} \left( 1 - \frac{101}{120} \right)$	<b>M1</b>	1.1b	
	$= \frac{19}{300} \text{ or } 0.0633\dots \text{ (accept awrt } 0.0633)$	<b>A1</b>	1.1b	
		<b>(4)</b>		

<b>c</b>	$P(T \cap D) = \frac{33}{100} \neq P(T) \times P(D) = \frac{2}{3} \times \frac{3}{5} = \frac{2}{5}$	<b>M1</b>	2.1	4th Understand and use the definition of independence in probability calculations.
	So, $T$ and $D$ are not statistically independent.	<b>A1</b>	2.4	
		<b>(2)</b>		

**(11 marks)**

**Notes**

**b ii** Alternative solution

$$P(T' \cap D') = 1 - P(T \cup D)$$

$$P(T \cup D) = \frac{2}{3} + \frac{3}{5} - \frac{33}{100}$$

$$= \frac{281}{300}$$

$$P(T' \cap D') = 1 - \frac{281}{300} = \frac{19}{300}$$

# A level Statistics & Mechanics: Practice Paper I mark scheme

<b>I6</b>	<b>Scheme</b>	<b>Marks</b>	<b>AOs</b>	<b>Pearson Progression Step and Progress descriptor</b>
<b>a</b>	A critical value is the point (or points) on the scale of the test statistic beyond which we reject the null hypothesis.	<b>B1</b>	1.2	5th Understand the language of hypothesis testing.
		<b>(1)</b>		
<b>b</b>	$H_0 : \rho = 0, H_1 : \rho > 0$ Critical value = 0.5494 $0.714 > 0.5494$ (test statistic in critical region) There is evidence to reject $H_0$ There is evidence that there is a positive correlation between the number of vehicles and road traffic accidents.	<b>B1</b> <b>M1</b> <b>A1</b>	2.5 1.1b 2.2b	6th Carry out a hypothesis test for zero correlation.
		<b>(3)</b>		
<b>c</b>	$r = -7.0 + 0.02v$	<b>B1</b>	1.2	4th Make predictions using the regression line within the range of the data.
		<b>(1)</b>		
<b>d</b>	Road fatalities per 100 000 population.	<b>B1</b>	1.2	2nd Know and understand the language of correlation and regression.
		<b>(1)</b>		
<b>e</b>	Outside the range of the data used in the model. or This would require extrapolation.	<b>B1</b>	3.5b	4th Understand the concepts of interpolation and extrapolation.
		<b>(1)</b>		
				<b>(7 marks)</b>
<b>Notes</b>				

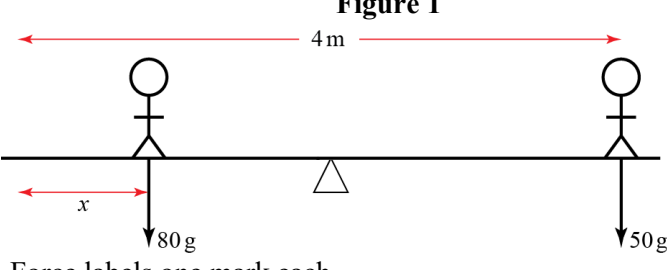
# A level Statistics & Mechanics: Practice Paper I mark scheme

I7	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
<b>a</b>	Moment from bus = $5000 \times 2 \times g$	<b>M1</b>	3.1a	5th Find resultant moments by considering direction.
	= $10\,000g$ (N m)	<b>A1</b>	1.1b	
	Moment from gold = $1000 \times 12 \times g$	<b>M1</b>	3.1b	
	= $12\,000g$ (N m)	<b>A1</b>	1.1b	
	Moment from people = $70 \times 8 \times n \times g$	<b>M1</b>	3.1a	
	= $560ng$ (N m)	<b>A1</b>	1.1b	
	Total moment = $(22\,000 - 560n)g$ (N m)	<b>A1</b>	1.1b	
		<b>(7)</b>		
<b>b</b>	Forming an equation or inequality for $n$ and solving to find ( $n = 39.28\dots$ )	<b>M1</b>	1.1b	5th Solve equilibrium problems involving horizontal bars.
	Need 40 people.	<b>A1</b>	3.2a	
		<b>(2)</b>		
<b>c</b>	New moment from gold and extra person is $1070 \times 12 \times g$ (N)	<b>M1</b>	3.1a	5th Solve equilibrium problems involving horizontal bars.
	New total moment = $(22840 - 560n)g$ (N m)	<b>M1</b>	1.1b	
	$n = 40.78\dots$	<b>A1</b>	3.2a	
	42 people (including the extra)	<b>A1</b>	2.4	
		<b>(4)</b>		
				<b>(13 marks)</b>



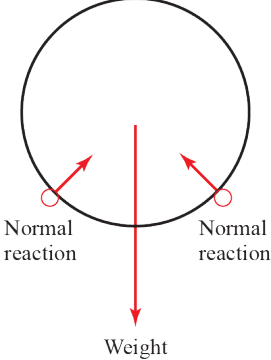
# A level Statistics & Mechanics: Practice Paper I mark scheme

18	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
<b>a</b>	Net force is $\mathbf{C} + \mathbf{W}$	<b>M1</b>	3.1b	4 <sup>th</sup>
	$= \begin{pmatrix} 5 \\ -1 \end{pmatrix}$	<b>A1</b>	1.1b	Calculate resultant forces using vectors.
		<b>(2)</b>		
<b>b</b>	Use of Newton's 2nd Law.	<b>M1</b>	3.1b	5 <sup>th</sup>
	$\mathbf{a} = \frac{F}{m}$	<b>M1</b>	1.1b	Use Newton's second law to model motion in two directions.
	$= \begin{pmatrix} 50 \\ -10 \end{pmatrix}$	<b>A1</b>	1.1b	
		<b>(3)</b>		
<b>c</b>	$\mathbf{s} = \mathbf{u}t + \frac{1}{2}\mathbf{a}t^2$	<b>M1</b>	1.1a	5 <sup>th</sup>
	$= \begin{pmatrix} 1 \\ 1 \end{pmatrix}t + \frac{1}{2}\begin{pmatrix} 50 \\ -10 \end{pmatrix}t^2$	<b>M1</b>	1.1b	Use the equations of motion to solve problems in familiar contexts.
	$x = t + 25t^2$	<b>A1</b>	1.1b	
	$y = t - 5t^2$	<b>A1</b>	1.1b	
		<b>(4)</b>		
<b>d</b>	Substitute $t = 10$	<b>M1</b>	3.1b	5 <sup>th</sup>
	$x = 2510$	<b>A1</b>	1.1b	Use the equations of motion to solve problems in familiar contexts.
	$y = -490$	<b>A1</b>	1.1b	
	Distance travelled = $\sqrt{2510^2 + (-490)^2}$	<b>M1</b>	1.1a	
	2557.38...(m) (Accept awrt 2560)	<b>A1</b>	3.2a	
		<b>(5)</b>		
<b>(14 marks)</b>				
<b>Notes</b>				

I9	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
a	<p style="text-align: center;"><b>Figure 1</b></p>  <p>Force labels one mark each Allow explicit evaluation with <math>g</math>.</p>	<b>B2</b>	2.5	4th Calculate moments.
	<b>(2)</b>			
b	Alice: Moment = $2 \times 50 \times g$	<b>M1</b>	1.1b	5th Calculate sums of moments.
	= $100g$ (N m)	<b>A1</b>	1.1b	
	Bob: Moment = $(2 - x) \times 80 \times g$	<b>M1</b>	3.4	
	= $80(2 - x)g$ (N m)	<b>A1</b>	1.1b	
	Total clockwise moment = $20g(4x - 3)$ (N m)	<b>A1</b>	1.1b	
<b>(5)</b>				
c	Equating to 0 and solving	<b>M1</b>	3.4	5th Solve equilibrium problems involving horizontal bars.
	$x = 0.75$ (m)	<b>A1</b>	1.1b	
	<b>(2)</b>			
d	Identifying 2 as a limit	<b>M1</b>	2.4	7th Solve problems involving bodies on the point of tilting.
	So tilts towards Alice when $0.75 < x \leq 2$	<b>A1</b>	2.2a	
	<b>(2)</b>			
e	Any valid limitation. For example, Pivot not a point. Alice can't sit exactly on the end. The see-saw might bend.	<b>A1</b>	3.5	3rd Understand assumptions common in mathematical modelling.
	<b>(1)</b>			

# A level Statistics & Mechanics: Practice Paper I mark scheme

I10	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
<b>a</b>	Use of $s = ut + \frac{1}{2}at^2$	<b>M1</b>	1.1a	6th Resolve velocity into horizontal and vertical components.
	Initial velocity is $(\cos \theta, \sin \theta)$	<b>A1</b>	3.4	
	$x = t \cos \theta$	<b>A1</b>	1.1b	
	$y = t \sin \theta - 5t^2$	<b>B1</b>	1.1b	
		<b>(4)</b>		
<b>b</b>	Solve $y = 0$ for $t$	<b>M1</b>	3.4	5th Model horizontal projection under gravity.
	$t(\sin \theta - 5t) = 0$	<b>A1</b>	1.1b	
	$t = 0$ or $t = \frac{\sin \theta}{5}$	<b>A1</b>	1.1b	
	$t = 0$ is initial position so $t = \frac{\sin \theta}{5}$	<b>M1</b>	2.4	
	$x = \frac{\cos \theta \sin \theta}{5} = \frac{2 \sin \theta \cos \theta}{10} = \frac{\sin 2\theta}{10}$	<b>A1</b>	1.1b	
		<b>(5)</b>		
<b>c</b>	Sketch of $\sin 2\theta$ or other legitimate method.	<b>M1</b>	2.2a	6th Resolve velocity into horizontal and vertical components.
	Maximum is at $\theta = 45^\circ$	<b>A1</b>	2.4	
		<b>(2)</b>		
<b>d</b>	Correct limitation. For example, air resistance.	<b>B1</b>	3.5b	3rd Understand assumptions common in mathematical modelling.
		<b>(1)</b>		
<b>(12 marks)</b>				
<b>Notes</b>				

I11	Scheme	Marks	AOs	Pearson Progression Step and Progress descriptor
a	 <p>One correct force with correct label. Two more correct forces with correct labels.</p>	<b>B1</b>	2.5	3rd Draw force diagrams.
	<b>B1</b>	2.5		
	<b>(2)</b>			
b	Resolve vertically.	<b>M1</b>	1.1b	5th Calculate resultant forces in perpendicular directions.
	Weight = 8g	<b>M1</b>	1.1b	
	= 78.4	<b>M1</b>	1.1b	
	Vertical part of normal reaction is $2R \cos 40$	<b>A1</b>	1.1b	
	$2R \cos 40 = 78.4$	<b>M1</b>	1.1b	
	Solve for $R$	<b>M1</b>	1.1b	
	$R = 51.171\dots$ (N) accept awrt 51	<b>A1</b>	1.1b	
	<b>(7)</b>			
	<b>(9 marks)</b>			