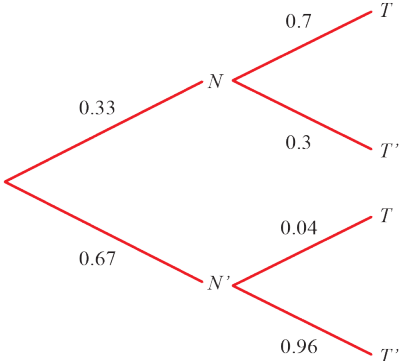


# A level Statistics & Mechanics: Practice Paper G mark scheme

| G1           | Scheme   | Marks      | AOs  | Pearson Progression Step and Progress descriptor                       |
|--------------|--|------------|------|--|
| <b>a</b>     | Linear association between $e$ and $f$ .   | <b>B1</b>  | 1.2  | 2nd<br>Know and understand the language of correlation and regression. |
|              |  | <b>(1)</b> |      |  |
| <b>b</b>     | It requires extropolation and hence it may be unreliable.  | <b>B1</b>  | 1.2  | 4th<br>Understand the concepts of interpolation and extrapolation.     |
|              |  | <b>(1)</b> |      |  |
| <b>c</b>     | Fuel consumption ( $f$ )   | <b>B1</b>  | 1.2  | 2nd<br>Know and understand the language of correlation and regression. |
|              |  | <b>(1)</b> |      |  |
| <b>d</b>     | A hypothesis test is a statistical test that is used to determine whether there is enough evidence in a <u>sample of data</u> to infer that a certain condition is true for the <u>entire population</u> .   | <b>B1</b>  | 1.2  | 5th<br>Understand the language of hypothesis testing.                  |
|              |  | <b>(1)</b> |      |  |
| <b>e</b>     | $H_0 : \rho = 0, H_1 : \rho < 0$<br>Critical value = $-0.3665$<br>$-0.803 < -0.3665$ (test statistic in critical region) Reject $H_0$<br>There is evidence that the product moment correlation coefficient for CO <sub>2</sub> emissions and fuel consumption is less than zero. | <b>B1</b>  | 2.5  | 6th<br>Carry out a hypothesis test for zero correlation.               |
|              |  | <b>M1</b>  | 1.1b |  |
|              |  | <b>A1</b>  | 2.2b |  |
|              |  | <b>(3)</b> |      |  |
|              |  |            |      | <b>(7 marks)</b>   |
| <b>Notes</b> |  |            |      |  |

# A level Statistics & Mechanics: Practice Paper G mark scheme

| G2               | Scheme   | Marks      | AOs  | Pearson Progression Step and Progress descriptor                           |
|------------------|--|------------|------|--|
| <b>a</b>         |  <p>Let <math>N \sim</math> new tyre and <math>T \sim</math> tracking<br/> <math>P(N) = 0.33</math> and <math>P(T) = 0.67</math><br/> <math>0.7, 0.3, 0.04</math> and <math>0.96</math></p> | <b>B1</b>  | 2.5  | 3rd<br>Draw and use tree diagrams with three branches and/or three levels. |
|                  |  | <b>B1</b>  | 1.1b |  |
|                  |  | <b>B1</b>  | 1.1b |  |
|                  |  | <b>(3)</b> |      |  |
| <b>b</b>         | $P(\text{exactly one defect}) = 0.33 \times 0.3 + 0.67 \times 0.04$  | <b>M1</b>  | 3.1b | 5th<br>Understand the language and notation of conditional probability.    |
|                  | $= 0.1258$   | <b>A1</b>  | 1.1b |  |
|                  |  | <b>(2)</b> |      |  |
| <b>c</b>         | $1 - P(\text{no defects}) = 1 - 0.67 \times 0.96 \times 0.65$  | <b>M1</b>  | 3.1b | 5th<br>Understand the language and notation of conditional probability.    |
|                  | $= 0.5819 \dots$ awrt $0.582$ (3 d.p.)   | <b>A1</b>  | 1.1b |  |
|                  |  | <b>(2)</b> |      |  |
| <b>d</b>         | To have their cars checked regularly as there is over a 50 % chance they need new tyres, tracking or brake pads.   | <b>B1</b>  | 3.2a | 5th<br>Understand the language and notation of conditional probability.    |
|                  |  | <b>(1)</b> |      |  |
| <b>(8 marks)</b> |  |            |      |  |
| <b>Notes</b>     |  |            |      |  |

# A level Statistics & Mechanics: Practice Paper G mark scheme

| <b>G3</b> | <b>Scheme</b>  | <b>Marks</b> | <b>AOs</b> | <b>Pearson Progression Step and Progress descriptor</b>   |
|-----------|--|--------------|------------|---|
| <b>a</b>  | Bell shaped.   | <b>B1</b>    | 2.2a       | 5th<br>Understand the basic features of the normal distribution including parameters, shape and notation. |
|           |  | <b>(1)</b>   |            |   |
| <b>b</b>  | $X \sim$ Daily mean pressure $X \sim N(1006, 4.4^2)$   | <b>M1</b>    | 3.3        | 5th<br>Calculate probabilities for the standard normal distribution using a calculator.                   |
|           | $P(X < 1000) = 0.0863$   | <b>A1</b>    | 1.1b       |   |
|           |  | <b>(2)</b>   |            |   |
| <b>c</b>  | A sensible reason. For example,<br>The tails of a Normal distribution are infinite.<br>Cannot rule out extreme events. | <b>B1</b>    | 2.4        | 5th<br>Understand the basic features of the normal distribution including parameters, shape and notation. |
|           |  | <b>(1)</b>   |            |   |

# A level Statistics & Mechanics: Practice Paper G mark scheme

|              |  |            |      |   |
|--------------|--|------------|------|---|
| <b>d</b>     | Comparison and sensible comment on means. For example,<br>The mean daily mean pressure for Beijing is less than Jacksonville.<br>This suggests better weather in Jacksonville. | <b>B1</b>  | 2.2b | 8th<br>Solve real-life problems in context using probability distributions. |
|              | Comparison and sensible comment on standard deviations. For example,<br>The standard deviation for Beijing is greater than that for Jacksonville.                              | <b>B1</b>  | 2.2b |   |
|              | This suggests more consistent weather in Jacksonville.   | <b>B1</b>  | 2.2b |   |
|              | Student claim could be correct.  | <b>B1</b>  | 2.2b |   |
|              |  | <b>(4)</b> |      |   |
|              |  |            |      | <b>(8 marks)</b>  |
| <b>Notes</b> |  |            |      |   |
| <b>a</b>     | Do not accept symmetrical with no discription of the shape.  |            |      |   |
| <b>d</b>     | B2 for Suggests better weather in Jacksonville but less consistent.  |            |      |   |

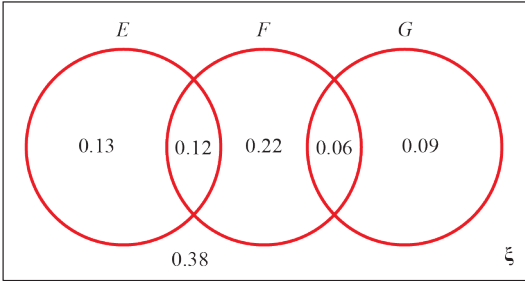
# A level Statistics & Mechanics: Practice Paper G mark scheme

| <b>G4</b> | <b>Scheme</b>  | <b>Marks</b>                        | <b>AOs</b>          | <b>Pearson Progression Step and Progress descriptor</b>                                    |
|-----------|--|-------------------------------------|---------------------|--|
| <b>a</b>  | Linear association between two variables.  | <b>B1</b>                           | 1.2                 | 2nd<br>Know and understand the language of correlation and regression.                     |
|           |  | <b>(1)</b>                          |                     |  |
| <b>b</b>  | Negative correlation.  | <b>B1</b>                           | 1.2                 | 2nd<br>Know and understand the language of correlation and regression.                     |
|           |  | <b>(1)</b>                          |                     |  |
| <b>c</b>  | As daily mean pressure increases (rises) daily mean wind speed decreases (falls) in Hurn May to October in 2015.<br>or<br>As daily mean pressure decreases (falls) daily mean wind speed increases (rises) in Hurn May to October in 2015. | <b>B1</b>                           | 3.2                 | 5th<br>Interpret the PPMC as a measure of correlation.                                     |
|           |  | <b>(1)</b>                          |                     |  |
| <b>d</b>  | $H_0 : \rho = 0, H_1 : \rho < 0$<br>$p$ -value $< 0.05$<br>There is evidence to reject $H_0$ .<br>There is (strong) evidence of negative correlation between the daily mean wind speed and daily mean pressure.                            | <b>B1</b><br><b>M1</b><br><b>A1</b> | 2.5<br>1.1b<br>2.2b | 6th<br>Carry out a hypothesis test for zero correlation.                                   |
|           |  | <b>(3)</b>                          |                     |  |
| <b>e</b>  | Daily mean wind speed = $180 - 0.170 \times$ daily mean pressure.  | <b>B2</b>                           | 1.1b                | 4th<br>Use the principles of bivariate data analysis in the context of the large data set. |
|           |  | <b>(2)</b>                          |                     |  |

# A level Statistics & Mechanics: Practice Paper G mark scheme

|                   |  |            |      |  |
|-------------------|--|------------|------|--|
| <b>f</b>          | The regression model suggests for every hPa increase in daily mean pressure the daily mean wind speed decreases by 0.1694 knots.<br>or<br>The regression model suggests for every hPa decrease in daily mean pressure the daily mean wind speed increases by 0.1694 knots. | <b>B1</b>  | 3.2  | 4th<br>Use the principles of bivariate data analysis in the context of the large data set. |
|                   |  | <b>(1)</b> |      |  |
| <b>g</b>          | Sensible comment. For example,<br>Not very accurate as very few or no points<br>Not very accurate as near the bottom range for the data.   | <b>B1</b>  | 3.5b | 4th<br>Make predictions using the regression line within the range of the data.            |
|                   |  | <b>(1)</b> |      |  |
| <b>(10 marks)</b> |  |            |      |  |
| <b>Notes</b>      |  |            |      |  |
| <b>e</b>          | B1 $y = 180.0 - 0.1694x$ unless $x$ and $y$ are defined.   |            |      |  |

# A level Statistics & Mechanics: Practice Paper G mark scheme

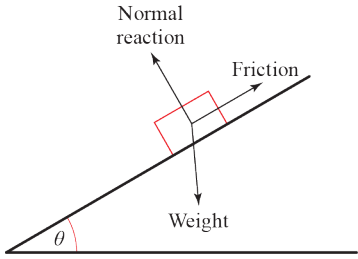
| G5                | Scheme   | Marks       | AOs         | Pearson Progression Step and Progress descriptor                                      |
|-------------------|--|-------------|-------------|---|
| <b>a</b>          | $P(E F') = \frac{P(E' \cap F')}{P(F')} \text{ or } \frac{0.47}{0.6}$               | <b>M1</b>   | 3.1a        | 4th<br>Calculate probabilities using set notation.                                    |
|                   | $= \frac{47}{60} \text{ or } 0.783 \text{ (3 s.f.)}$                               | <b>A1</b>   | 1.1b        |   |
|                   |  | <b>(2)</b>  |             |   |
| <b>B</b>          | $P(E) \times P(F) = 0.25 \times 0.4 = 0.1 \neq P(E \cap F) = 0.12$                 | <b>M1</b>   | 2.1         | 4th<br>Understand and use the definition of independence in probability calculations. |
|                   | So, $E$ and $F$ are not statistically independent.                                 | <b>A1</b>   | 2.4         |   |
|                   |  | <b>(2)</b>  |             |   |
| <b>c</b>          |  | <b>B1</b>   | 2.5         | 3rd<br>Understand and use Venn diagrams for multiple events.                          |
|                   | Use of independence and all values in $G$ correct.<br>All values correct.          | <b>M1A1</b> | 3.1a        |   |
|                   |  |             | <b>M1A1</b> | 1.1b<br>1.1b<br>1.1b  |
|                   |  | <b>(5)</b>  |             |   |
| <b>d</b>          | $P([F \cup G]') = 0.13 + 0.38$   | <b>M1</b>   | 3.1a        | 4th<br>Calculate probabilities using set notation.                                    |
|                   | $= 0.51$   | <b>A1</b>   | 1.1b        |   |
|                   |  | <b>(2)</b>  |             |   |
| <b>(11 marks)</b> |  |             |             |   |
| <b>Notes</b>      |  |             |             |   |

# A level Statistics & Mechanics: Practice Paper G mark scheme

| G6               | Scheme  | Marks     | AOs  | Pearson Progression Step and Progress descriptor                           |
|------------------|---|-----------|------|--|
|                  | $X \sim B(200, 0.54)$                                     | <b>B1</b> | 3.3  | 7th<br>Use the normal distribution to approximate a binomial distribution. |
|                  | $Y \sim N(108, 49.68)$                                    | <b>B2</b> | 3.1b |  |
|                  | $P(X > 100) = P(X \geq 101)$                              | <b>M1</b> | 3.4  |  |
|                  | $= P\left(Z \geq \frac{100.5 - 108}{\sqrt{49.68}}\right)$ | <b>M1</b> | 1.1b |  |
|                  | $= P(Z \geq -1.06\dots) = 0.8554$                         | <b>A1</b> | 1.1b |  |
| <b>(6 marks)</b> |   |           |      |  |
| <b>Notes</b>     |   |           |      |  |



| G7 | Scheme  | Marks     | AOs  | Pearson Progression Step and Progress descriptor             |
|----|---|-----------|------|--|
|    | Moment on see-saw is force $\times$ distance from pivot.            | <b>M1</b> | 1.1a | 5th<br>Solve equilibrium problems involving horizontal bars. |
|    | Moment on Poppy's see-saw due to Poppy is $pg \times 3 = 3pg$ (N m) | <b>M1</b> | 2.2a |  |
|    | Force on Bob due to Poppy is $\frac{3pg}{2}$ (N)                    | <b>A1</b> | 2.2a |  |
|    | Force on Bob due to Quentin is $\frac{3qg}{2}$ (N)                  | <b>A1</b> | 2.2a |  |
|    | Total force on Bob is $\frac{3}{2}(p+q)g$ (N)                       | <b>M1</b> | 2.2a |  |
|    | Weight of Bob is 80g (N)  | <b>M1</b> | 1.1b |  |
|    | Forces are equal so $\frac{3}{2}(p+q)g = 80g$                       | <b>M1</b> | 3.1b |  |
|    | $p + q = 53$ to the nearest whole number.                           | <b>A1</b> | 2.4  |  |
|    |   |           |      | <b>(8 marks)</b>   |

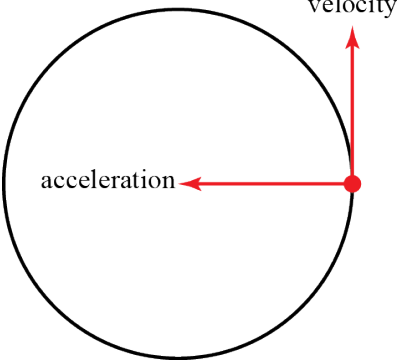
| G8 | Scheme   | Marks                  | AOs  | Pearson Progression Step and Progress descriptor |
|----|--|------------------------|------|--|
| a  |  <p>B1 for each correct force with correct label.</p> | <b>B3</b>              | 2.5  | 3rd<br>Draw force diagrams.                      |
|    |  | <b>(3)</b>             |      |  |
| b  | Resolve horizontally/vertically or along/perp to plane.  | <b>M1</b>              | 1.1b | 7th<br>The concept of limiting equilibrium.      |
|    | $R = 3g \cos \theta$   | <b>A1</b>              | 1.1b |  |
|    | $F = 3g \sin \theta$   | <b>A1</b>              | 1.1b |  |
|    | Limiting equilibrium means $\mu R = F$<br>$\mu R = 3\mu g \cos \theta$   | <b>A1</b>              | 1.1b |  |
|    | $3\mu g \cos \theta = 3g \sin \theta$  | <b>M1</b>              | 1.1b |  |
|    | $\mu = \tan \theta$  | <b>A1</b>              | 1.1b |  |
|    | <b>(6)</b>   |                        |      |  |
| c  | $\tan 30 = 0.577\dots$   | <b>A1</b>              | 3.1a | 7th<br>The concept of limiting equilibrium.      |
|    | For limiting equilibrium, $\mu = 0.577\dots$   | <b>M1</b>              | 3.1a |  |
|    | But $\mu = 0.3$ so less friction.  | <b>M1</b>              | 3.1a |  |
|    | Hence the object slips.  | <b>A1</b>              | 3.2a |  |
|    |  | <b>(4)</b>             |      |  |
| d  | No object would remain in equilibrium, because normal reaction becomes zero.   | <b>B1</b><br><b>A1</b> | 3.2a | 7th<br>The concept of limiting equilibrium.      |
|    |  | <b>(2)</b>             |      |  |
|    |  |                        |      | <b>(15 marks)</b>                                |

# A level Statistics & Mechanics: Practice Paper G mark scheme

| <b>G9</b>    | <b>Scheme</b>  | <b>Marks</b> | <b>AOs</b> | <b>Pearson Progression Step and Progress descriptor</b> |
|--------------|--|--------------|------------|---|
|              | Suvat equation.  | <b>M1</b>    | 3.1a       | 8th<br>Derive formulae for projectile motion.           |
|              | $y = 8t \sin 60 - \frac{1}{2}gt^2$                               | <b>M1</b>    | 1.1b       |   |
|              | $= 4\sqrt{3}t - 4.9t^2$ (allow awrt 6.9)                         | <b>A1</b>    | 1.1b       |   |
|              | Solve $y = 2$  | <b>M1</b>    | 1.1a       |   |
|              | $t = 0.404\dots$ or $t = 1.009\dots$ (accept awrt 0.40 and 1.01) | <b>A2</b>    | 1.1b       |   |
|              | Time spent above 2 m is difference.                              | <b>M1</b>    | 2.4        |   |
|              | 0.605... (s) (accept awrt 0.61)                                  | <b>A1ft</b>  | 3.4a       |   |
|              |  |              |            | <b>(8 marks)</b>  |
| <b>Notes</b> |  |              |            |   |

# A level Statistics & Mechanics: Practice Paper G mark scheme

| G10               | Scheme   | Marks                  | AOs        | Pearson Progression Step and Progress descriptor                  |
|-------------------|--|------------------------|------------|---|
| <b>a</b>          | Resultant force is $\mathbf{A} + \mathbf{B}$   | <b>M1</b>              | 3.1b       | 5th<br>Use Newton's second law to model motion in two directions. |
|                   | $= 3\mathbf{i} - \mathbf{j}$ (N)   | <b>A1</b>              | 1.1b       |   |
|                   | Use of Newton's 2nd Law.   | <b>M1</b>              | 3.1b       |   |
|                   | $\mathbf{a} = \frac{F}{m}$   | <b>M1</b>              | 1.1b       |   |
|                   | $6\mathbf{i} - 2\mathbf{j}$ ( $\text{m s}^{-2}$ )  | <b>A1</b>              | 1.1b       |   |
|                   | $\mathbf{s} = \mathbf{s}_0 + \frac{1}{2}\mathbf{a}t^2$   | <b>M1</b>              | 1.1a       |   |
|                   | $= 3\mathbf{i} + 4\mathbf{j} + \frac{1}{2}(6\mathbf{i} - 2\mathbf{j})t^2$  | <b>M1</b>              | 1.1b       |   |
|                   | $x = 3 + 3t^2$   | <b>A1</b>              | 1.1b       |   |
|                   | $y = 4 - t^2$  | <b>A1</b>              | 1.1b       |   |
|                   |  | <b>(9)</b>             |            |   |
| <b>b</b>          | $x = 3 + 3t^2 > 0$ for all $t > 0$   | <b>M1</b>              | 2.4        | 4th<br>Complete proofs by deduction and direct algebraic methods. |
|                   | so $x \neq 3$  | <b>A1</b>              | 2.2a       |   |
|                   |  | <b>(2)</b>             |            |   |
| <b>c</b>          | Anything reasonable. For example, a ball in a river with wind.<br>Descriptions of $\mathbf{A}$ and $\mathbf{B}$ .<br>For example, $\mathbf{A}$ is force due to water.<br>For example, $\mathbf{B}$ is force due to wind. | <b>B1</b><br><b>B1</b> | 3.5<br>3.5 | 3rd<br>Understand assumptions common in mathematical modelling.   |
|                   |  | <b>(2)</b>             |            |   |
| <b>(13 marks)</b> |  |                        |            |   |
| <b>Notes</b>      |  |                        |            |   |
| <b>b</b>          | Accept any valid argument (For example, equivalent argument for $y$ )  |                        |            |   |

| G11  | Scheme   | Marks      | AOs  | Pearson Progression Step and Progress descriptor                               |
|--|--|------------|------|--|
| <b>a</b>   | Differentiate $\mathbf{r}$ w.r.t. time   | <b>M1</b>  | 1.1a | 8th<br>Solve general kinematics problems using calculus of vectors.            |
|  | $\mathbf{v} = \begin{pmatrix} -2 \sin 2t \\ 2 \cos 2t \end{pmatrix}$   | <b>A1</b>  | 1.1b |  |
|  | $\mathbf{a} = \begin{pmatrix} -4 \cos 2t \\ -4 \sin 2t \end{pmatrix}$  | <b>A1</b>  | 1.1b |  |
|  |  | <b>(3)</b> |      |  |
| <b>b</b>   | $\mathbf{a} = -4 \begin{pmatrix} \cos 2t \\ \sin 2t \end{pmatrix} = -4\mathbf{r}$  | <b>B1</b>  | 2.2a | 8th<br>Solve general kinematics problems in a range of contexts using vectors. |
|  |  | <b>(1)</b> |      |  |
| <b>c</b>   |  <p>Diagram of circular orbit with velocity tangent to circle and acceleration pointing towards centre. Velocity must be in vertical direction.</p> | <b>B1</b>  | 2.5  | 8th<br>Solve general kinematics problems in a range of contexts using vectors. |
|  |  | <b>B1</b>  | 2.5  |  |
|  |  | <b>(2)</b> |      |  |
|  |  |            |      | <b>(6 marks)</b>   |
| <b>Notes</b>   |  |            |      |  |
| <b>c</b><br>B1 for correct velocity direction<br>B1 for correct acceleration direction |  |            |      |  |