

<b>1.</b>	Considers the expression $x^2 + \frac{13}{2}x + 16$ either on its own or as part of an inequality/equation with 0 on the other side.	<b>M1</b>
	Makes an attempt to complete the square. For example, stating: $\left(x + \frac{13}{4}\right)^2 - \frac{169}{16} + \frac{256}{16}$ (ignore any (in)equation)	<b>M1</b>
	States a fully correct answer: $\left(x + \frac{13}{4}\right)^2 + \frac{87}{16}$ (ignore any (in)equation)	<b>A1</b>
	Interprets this solution as proving the inequality for all values of $x$ . Could, for example, state that $\left(x + \frac{13}{4}\right)^2 \geq 0$ as a number squared is always positive or zero, therefore $\left(x + \frac{13}{4}\right)^2 + \frac{87}{16} > 0$ . Must be logically connected with the statement to be proved; this could be in the form of an additional statement. So $x^2 + 6x + 18 > 2 - \frac{1}{2}x$ (for all $x$ ) or by a string of connectives which must be equivalent to “if and only if”s.	<b>A1</b>
		<b>Total: 4 marks</b>

**NOTE:** Any correct and complete method is acceptable for demonstrating that  $x^2 + \frac{13}{2}x + 16 > 0$  for all  $x$ .

(e.g. finding the discriminant and single value,  
finding the minimum point by differentiation  
or completing the square and showing that it is both positive and a minimum, sketching the graph supported with appropriate methodology etc).

<b>2a</b>	$m = \frac{11 - (-7)}{-6 - 4} = \frac{18}{-10} = -\frac{9}{5}$	<b>B1</b>
<p>Correct substitution of (4, -7) or (-6, 11) and their gradient into <math>y = mx + b</math> or <math>y - y_1 = m(x - x_1)</math> o.e. to find the equation of the line.</p> <p>For example, <math>-7 = \left(-\frac{9}{5}\right)(4) + b</math> or <math>y + 7 = -\frac{9}{5}(x - 4)</math> or <math>11 = \left(-\frac{9}{5}\right)(-6) + b</math> or <math>y - 11 = -\frac{9}{5}(x + 6)</math>.</p>		<b>M1</b>
$5y + 9x - 1 = 0$ or $-5y - 9x + 1 = 0$ only		<b>A1</b>
		<b>(3 marks)</b>
<b>2b</b>	$y = 0, x = \frac{1}{9}$ so $A\left(\frac{1}{9}, 0\right)$ . Award mark for $x = \frac{1}{9}$ seen.	<b>B1</b>
$x = 0, y = \frac{1}{5}$ so $B\left(0, \frac{1}{5}\right)$ . Award mark for $y = \frac{1}{5}$ seen.		<b>B1</b>
Area = $\frac{1}{2} \times \frac{1}{5} \times \frac{1}{9} = \frac{1}{90}$		<b>B1</b>
		<b>(3 marks)</b>
		<b>Total: 6 marks</b>

<b>3</b>	Makes an attempt to begin solving the equation. For example, states that $\frac{\sin(3\theta + 20^\circ)}{\cos(3\theta + 20^\circ)} = \frac{4}{4\sqrt{3}}$	<b>M1</b>
Uses the identity $\tan \theta = \frac{\sin \theta}{\cos \theta}$ to write, $\tan(3\theta + 20^\circ) = \frac{4}{4\sqrt{3}} = \frac{1}{\sqrt{3}}$		<b>M1</b>
States or implies use of the inverse tangent. For example, $3\theta + 20^\circ = \tan^{-1}\left(\frac{1}{\sqrt{3}}\right)$ or $3\theta + 20^\circ = 30^\circ$		<b>M1</b>
Shows understanding that there will be further solutions in the given range, by adding $180^\circ$ to $30^\circ$ at least once. $3\theta + 20^\circ = 30^\circ, 210^\circ, 390^\circ, \dots$ (ignore any out of range values).		<b>M1</b>
Subtracts 20 and divides each answer by 3. $\theta = \left(\frac{10}{3}\right)^\circ, \left(\frac{190}{3}\right)^\circ, \left(\frac{370}{3}\right)^\circ, \dots$ (ignore any out of range values).		<b>M1</b>
States the correct final answers to 1 decimal place. $3.3^\circ, 63.3^\circ, 123.3^\circ$ cao		<b>A1</b>

<b>4</b>	Uses appropriate law of logarithms to write $\log_{11}(2x-1)(x+4)=1$	<b>M1</b>
	Inverse $\log_{11}$ (or 11 to the) both sides. $(2x-1)(x+4)=11$	<b>M1</b>
	Derives a 3 term quadratic equation. $2x^2 + 7x - 15 = 0$	<b>M1</b>
	Correctly factorises $(2x-3)(x+5)=0$ or uses appropriate technique to solve their quadratic.	<b>M1</b>
	Solves to find $x = \frac{3}{2}$	<b>A1</b>
	Understands that $x \neq -5$ stating that this solution would require taking the log of a negative number, which is not possible.	<b>B1</b>
<b>Total:</b> <b>6 marks</b>		

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<b>5a</b>	Equates the <b>i</b> components for the equation $\mathbf{a} + \mathbf{b} = m\mathbf{c}$ o.e. $2p + 6 = 4m$	<b>B1</b>
	Equates the <b>j</b> components for the their equation $\mathbf{a} + \mathbf{b} = m\mathbf{c}$ $-5 - 3p = -5m$	<b>B1</b>
	Makes an attempt to find $p$ by eliminating $m$ in some way. For example, $\frac{10p+30}{20+12p} = \frac{20m}{20m}$ o.e. or $\frac{2p+6}{-5-3p} = -\frac{4}{5}$ o.e.	<b>M1</b>
	$p = 5$	<b>A1</b>
	<b>NOTES:</b> Alternatively, M1: attempt to eliminate $p$ first. A1: $m = 4$ and $p = 5$	<b>(4 marks)</b>
<b>5b</b>	Using their value for $p$ from above, makes a substitution into the vectors to form $\mathbf{a} + \mathbf{b}$ $10\mathbf{i} - 5\mathbf{j} + 6\mathbf{i} - 15\mathbf{j}$	<b>M1ft</b>
	Correctly simplifies. $16\mathbf{i} - 20\mathbf{j}$	<b>A1ft</b>
	<b>NOTES: OR</b> M1ft: substitute their $m = 4$ into their $\mathbf{a} + \mathbf{b} = m\mathbf{c}$ . A1ft: correct simplification.	<b>(2 marks)</b>
<b>Total:</b> <b>6 marks</b>		

<b>6a</b>	Makes an attempt to substitute 7 into the equation, for example, $P = 100e^{0.4 \times 7}$ seen.	<b>M1</b>
	1644 or 1640 only (do not accept non-integeric final answer).	<b>A1</b>
		<b>(2 marks)</b>
<b>6b</b>	It is the initial bacteria population.	<b>B1</b>
		<b>(1 mark)</b>
<b>6c</b>	States that $100e^{0.4t} > 1000000$ or that $e^{0.4t} > 10000$	<b>M1</b>
	Solves to find $t > \frac{\ln(10000)}{0.4}$	<b>M1</b>
	24 (hours) cao (do not accept e.g. 24.0).	<b>A1</b>
		<b>(3 marks)</b>
		<b>Total: 6 marks</b>

<b>7</b>	$y = mx - 2$ seen or implied.	<b>M1</b>
	Substitutes their $y = mx - 2$ into $x^2 + 6x + y^2 - 8y = 4$ $x^2 + 6x + (mx - 2)^2 - 8(mx - 2) = 4$ o.e.	<b>M1</b>
	Rearranges to a 3 term quadratic in $x$ (condone one arithmetic error). $(1 + m^2)x^2 + (6 - 12m)x + 16 = 0$	<b>M1</b>
	Uses $b^2 - 4ac = 0, (6 - 12m)^2 - (4)(1 + m^2)(16) = 0$	<b>M1</b>
	Rearranges to $20m^2 - 36m - 7 = 0$ or any multiple of this.	<b>A1</b>
	Attempts solution using valid method. For example, $m = \frac{36 \pm \sqrt{(-36)^2 - (4)(20)(-7)}}{2(20)}$	<b>M1</b>
	$m = \frac{9}{10} \pm \frac{\sqrt{29}}{5}$ or $m = \frac{9 \pm 2\sqrt{29}}{10}$ o.e. (NB decimals A0).	<b>A1</b>
		<b>Total: 7 marks</b>

**NOTES:** Elimination of  $x$  follows the same scheme.  $x = \frac{y+2}{m}$  leading to  $\left(\frac{y+2}{m}\right)^2 + 6\left(\frac{y+2}{m}\right) + y^2 - 8y = 4$

$$\text{This leads to } (1 + m^2)y^2 + (4 + 6m - 8m^2)y + 4 + 12m - 4m^2 = 0$$

Use of  $b^2 - 4ac = 0$  gives  $(4 + 6m - 8m^2)^2 - (4)(1 + m^2)(4 + 12m - 4m^2) = 0$  which reduces to  $4m^2(20m^2 - 36m - 7) = 0$ .  $m$  cannot equal 0, so this must be discarded as a solution for the final A mark.

$b^2 - 4ac = 0$  could be used implicitly within the quadratic equation formula.

<b>8a</b>	Makes an attempt to find the vector $\overrightarrow{AB}$ .	<b>M1</b>
	For example, writing $\overrightarrow{AB} = \overrightarrow{OB} - \overrightarrow{OA}$ or $\overrightarrow{AB} = 10\mathbf{i} + q\mathbf{j} - (4\mathbf{i} + 7\mathbf{j})$	
	Shows a fully simplified answer: $\overrightarrow{AB} = 6\mathbf{i} + (q - 7)\mathbf{j}$	<b>A1</b>
		<b>(2 marks)</b>
<b>8b</b>	Correctly interprets the meaning of $ \overrightarrow{AB}  = 2\sqrt{13}$ , by writing $(6)^2 + (q - 7)^2 = (2\sqrt{13})^2$ o.e.	<b>M1</b>
	Correct method to solve quadratic equation in $q$ (full working must be shown).	<b>M1</b>
	For example, $(q - 7)^2 = 16$ or $q^2 - 14q + 33 = 0$	
	$q - 7 = \pm 4$ or $(q - 11)(q - 3) = 0$ or $q = \frac{14 \pm \sqrt{14^2 - 4 \times 1 \times 33}}{2 \times 1}$	<b>M1</b>
	$q = 11$	<b>A1</b>
	$q = 3$	<b>A1</b>
		<b>(5 marks)</b>
		<b>Total: 7 marks</b>

<b>9a</b>	States or implies the expansion of a binomial expression to the 9th power, up to and including the $x^3$ term.	<b>M1</b>
	$(a+b)^9 = {}^9C_0a^9 + {}^9C_1a^8b + {}^9C_2a^7b^2 + {}^9C_3a^6b^3 + \dots$ or $(a+b)^9 = a^9 + 9a^8b + 36a^7b^2 + 84a^6b^3 + \dots$	
	Correctly substitutes 2 and $px$ into the formula.	<b>M1</b>
	$(2+px)^9 = 2^9 + 9 \times 2^8 \times px + 36 \times 2^7 \times (px)^2 + 84 \times 2^6 \times (px)^3 + \dots$	
	Makes an attempt to simplify the expression (at least one power of 2 calculated and one bracket expanded correctly).	<b>M1dep</b>
	$(2+px)^9 = 512 + 9 \times 256 \times px + 36 \times 128 \times p^2x^2 + 84 \times 64 \times p^3x^3 + \dots$	
	States a fully correct answer: $(2+px)^9 = 512 + 2304px + 4608p^2x^2 + 5376p^3x^3 + \dots$	<b>A1</b>
		<b>(4 marks)</b>
<b>9bi</b>	States that $5376p^3 = -84$	<b>M1ft</b>
	Correctly solves for $p$ : $p^3 = -\frac{1}{64}$ so $p = -\frac{1}{4}$	<b>A1ft</b>
<b>9bi</b>	Correctly find the coefficient of the $x$ term: $2304 \left(-\frac{1}{4}\right) = -576$	<b>B1ft</b>
	Correctly find the coefficient of the $x^2$ term: $4608 \left(-\frac{1}{4}\right)^2 = 288$	<b>B1ft</b>
		<b>(4 marks)</b>
		<b>Total: 8 marks</b>

**NOTES:** ft marks – pursues a correct method and obtains a correct answer or answers from their 5376 from part a.

<b>10a</b>	States or implies that the angle at $P$ is $74^\circ$	<b>B1</b>
	States or implies the use of the cosine rule. For example, $p^2 = q^2 + r^2 - 2qr \cos P$	<b>M1</b>
	Makes substitution into the cosine rule. $p^2 = 7^2 + 15^2 - 2 \times 7 \times 15 \cos 74^\circ$	<b>M1ft</b>
	Makes attempt to simplify, for example, stating $p^2 = 216.11\dots$	<b>M1ft</b>
	States the correct final answer. $QR = 14.7$ km.	<b>A1</b>
		<b>(5 marks)</b>
<b>10b</b>	States or implies use of the sine rule, for example, writing $\frac{\sin Q}{q} = \frac{\sin P}{p}$	<b>M1</b>
	Makes an attempt to substitute into the sine rule. $\frac{\sin Q}{15} = \frac{\sin 74^\circ}{14.7}$	<b>M1ft</b>
	Solves to find $Q = 78.77\dots^\circ$	<b>A1ft</b>
	Makes an attempt to find the bearing, for example, writing bearing = $180^\circ - 78.77\dots^\circ - 33^\circ$	<b>M1ft</b>
	States the correct 3 figure bearing as $068^\circ$	<b>A1ft</b>
		<b>(5 marks)</b>
		<b>Total: 10 marks</b>

**NOTES:** **10a:** Award ft marks for correct use of cosine rule using an incorrect initial angle.

**10b:** Award ft marks for a correct solution using their answer to part (a).



<b>11a</b>	States or implies that area of base is $x^2$ .	<b>M1</b>	
	States or implies that total surface area of the fish tank is $x^2 + 4xh = 1600$ Use of a letter other than $h$ is acceptable.	<b>M1</b>	
	$h = \frac{400}{x} - \frac{x}{4}$	<b>M1</b>	
	Substitutes for $h$ in $V = x^2h = x^2 \left( \frac{400}{x} - \frac{x}{4} \right)$	<b>M1</b>	
	Simplifies to obtain $V = 400x - \frac{x^3}{4}$ *	<b>A1*</b>	
		<b>(5 marks)</b>	
<b>11b</b>	Differentiates $f(x)$	$\frac{dV}{dx} = 400 - \frac{3x^2}{4}$	<b>B1</b>
	Attempts to solve $\frac{dV}{dx} = 0$	$400 - \frac{3x^2}{4} = 0 \text{ or } 400 = \frac{3x^2}{4}$	<b>M1</b>
	$x = \frac{40\sqrt{3}}{3}$ o.e. (NB must be positive)		<b>A1</b>
	Substitutes for $x$ in $V = 400x - \frac{x^3}{4}$	$V_{\max/\min} = \frac{32\,000\sqrt{3}}{9}$ o.e. or awrt 6160	<b>A1</b>
			<b>(4 marks)</b>
<b>11c</b>	Differentiates $f'(x)$	$\frac{d^2V}{dx^2} = -\frac{3x}{2}$ o.e.	<b>M1</b>
	Substitutes $x = \frac{40\sqrt{3}}{3}$ into $f''(x)$	States $\frac{d^2V}{dx^2} < 0$ , so $V$ in part <b>b</b> is a maximum value.	<b>A1</b>
			<b>(2 marks)</b>
			<b>Total: 11 marks</b>

**NOTES: (a):** A sketch of a rectangular prism with a base of  $x$  by  $x$  and a height of  $h$  is acceptable for the first method mark.

**(c):** Other complete methods for demonstrating that  $V$  is a maximum are acceptable.

For example a sketch of the graph of  $V$  against  $x$  or calculation of values of  $V$  or  $\frac{dV}{dx}$  on either side.

<b>12a</b>	Attempts to take out $x$ or $-x$ .	$y = x(-x^2 + 2x + 8)$ or $y = -x(x^2 - 2x - 8)$	<b>M1</b>
	Fully and correctly factorised cubic.	$y = x(4-x)(2+x)$ or $y = -x(x-4)(x+2)$	<b>M1</b>
	Correct coordinates written. $A(-2,0)$ and $B(4, 0)$ .		<b>A1</b>
			<b>(3 marks)</b>
<b>12b</b>	Makes an attempt to find $\int (-x^3 + 2x^2 + 8x)dx$		<b>M1</b>
	Raising at least one $x$ power by 1 would constitute an attempt.		
	Fully correct integration seen.	$\left[ -\frac{x^4}{4} + \frac{2}{3}x^3 + 4x^2 \right]_{-2}^0$ (ignore limits at this stage)	<b>A1</b>
	Makes an attempt to substitute limits into integrated function to find the area between $x = -2$ and $x = 0$	$(0) - \left( -4 - \frac{16}{3} + 16 \right)$	<b>M1</b>
	Finds the correct answer.	$-\frac{20}{3}$	<b>A1</b>
	$+\frac{20}{3}$ stated or used as area here or later in solution (could be implied by correct final answer).		<b>B1</b>
	Makes an attempt to substitute limits into integrated function to find the area between $x = 0$ and $x = 4$	$\left( -64 + \frac{128}{3} + 64 \right) - (0)$	<b>M1</b>
	Finds the correct answer.	$\frac{128}{3}$	<b>A1</b>
	Correctly adds the two areas. $\frac{148}{3}$ o.e.		<b>A1</b>
			<b>(8 marks)</b>
			<b>Total: 11 marks</b>

**NOTES:**

**12a:** Award method marks for substituting limits even if evaluation at  $x = 0$  is not seen.

**12b:** For the first integral, candidates may integrate  $-f(x)$  between  $-2$  and  $0$  to obtain a positive answer directly.

<b>13a</b>	<p>Attempt to solve <math>q(x) = 0</math> by completing the square or by using the formula.</p> $x^2 - 10x - 20 = 0$ $(x - 5)^2 - 45 = 0$ <p>or</p> $x = \frac{10 \pm \sqrt{100 - 4(1)(-20)}}{2(1)}$	M1	
	$x = 5 \pm 3\sqrt{5}$ and/or statement that says $a = 5$ and $b = 5$	A1	
		<b>(2 marks)</b>	
<b>13b</b>	<p><b>Figure 1</b></p>	<p><math>q(0) = -20</math>, so <math>y = q(x)</math> intersects <math>y</math>-axis at <math>(0, -20)</math> and <math>x</math>-intercepts labelled (accept incorrect values from part a).</p>	B1ft
		<p><math>y = p(x)</math> intersects <math>y</math>-axis at <math>(0, 3)</math>.</p>	B1
		<p><math>y = p(x)</math> intersects <math>x</math>-axis at <math>(6, 0)</math>.</p>	B1
		<p>Graphs drawn as shown with all axes intercepts labelled. The two graphs should clearly intersect at two points, one at a negative value of <math>x</math> and one at a positive value of <math>x</math>. These points of intersection do not need to be labelled.</p>	B1
		<b>(4 marks)</b>	

<b>13c</b>	Statement indicating that this is the point where $p(x) = q(x)$ or $x^2 - 10x - 20 = 3 - \frac{1}{2}x$ seen.	<b>M1</b>
	Their equation factorised, or attempt to solve their equation by completing the square. $2x^2 - 19x - 46 = 0$ $(2x - 23)(x + 2) = 0$	<b>M1</b>
	$\left(\frac{23}{2}, -\frac{11}{4}\right)$	<b>A1</b>
	$(-2, 4)$	<b>A1</b>
		<b>(4 marks)</b>
<b>13d</b>	$x < -2$ or $x > \frac{23}{2}$ o.e.	<b>B1</b>
	$\{x: x \in \mathbb{R}, x < -2\} \cup \{x: x \in \mathbb{R}, x > 11.5\}$ <b>NB:</b> Must see “or” or $\cup$ (if missing SC1 for just the correct inequalities).	<b>B1</b>
		<b>(2 marks)</b>
		<b>Total: 12 marks</b>

**NOTES:**

**13a:** Equation can be solved by completing the square or by using the quadratic formula. Either method is acceptable.

**13b:** Answers with incorrect coordinates lose accuracy marks as appropriate. However, the graph accuracy marks can be awarded for correctly labelling their coordinates, even if their coordinates are incorrect.

**13c:** If the student incorrectly writes the initial equation, award 1 method mark for an attempt to solve the incorrect equation. Solving the correct equation by either factorising or completing the square is acceptable.

**(TOTAL: 100 MARKS)**